## Strategic Professional - Options

## Advanced Financial <br> Management (AFM)

September/December 2019 Sample Questions


AFM ACCA

Time allowed: 3 hours 15 minutes

This question paper is divided into two sections:
Section A - This ONE question is compulsory and MUST be attempted
Section B - BOTH questions are compulsory and MUST be attempted
Formulae and tables are on pages 8-12.
Do NOT open this question paper until instructed by the supervisor.

This question paper must not be removed from the examination hall.


The Association of Chartered Certified

## Section A - This ONE question is compulsory and MUST be attempted

1 Okan Co, a large listed company located in Yasailand whose currency is the $Y \$$, manufactures engines and engine parts. It is considering whether or not to invest in one of two new four-year projects: Project Alpha or Project Beta. Details of both projects are given separately. Previously, Okan Co has used relevant risk-adjusted discount rates to calculate the net present value (NPV) of projects. However, the finance director believes that calculating adjusted present values (APV) of projects would be more appropriate. Okan Co wants to base its decision on which project to invest in, on the returns generated by the projects, the projects' risk as measured by their project durations, and important non-financial aspects. Both projects are due to commence in six months' time.

## Funding for projects Alpha and Beta

Project Alpha or Project Beta will each require the same amount of initial funding of $\mathrm{Y} \$ 50,000,000$.
Proceeds from the sale of a factory based in Europe in six months' time, for Euro ( $(1) 10,000,000$, will provide part of the funding and the balance will be financed by debt borrowing.

Okan Co expects to hedge the $€ 10,000,000$ using either forward markets or money markets. The following information is available on these markets:

## Foreign exchange rates

$Y \$ / € 1$
2.5210-2.5862

Spot
2.5462-2.6121

## Bank interest rates

|  | Investing | Borrowing |
| :--- | :---: | :---: |
| Yasailand | $2.40 \%$ | $5 \cdot 00 \%$ |
| Eurozone | $1.05 \%$ | $2.20 \%$ |

The balance of funding raised by domestic debt borrowing will be through a four-year subsidised loan on which interest is payable at $2 \cdot 1 \%$, although Okan Co's normal borrowing rate is $5 \%$.

Issue costs related to raising this finance will be 3\% of the gross proceeds.

## Project Alpha details

Project Alpha's base case NPV and APV, in six months' time when the project will commence, should be estimated using the following information.

The sales revenues and production costs related to Project Alpha in six months' time, before any annual price or cost increases, are estimated as follows:

| Year | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | ---: |
| Sales revenue (Y\$ 000s) | 15,750 | 28,350 | 47,250 | 23,100 |
| Production cost (Y\$ 000s) | 6,120 | 10,710 | 21,420 | 8,160 |

It is expected that the sales price will increase at an annual inflation rate of $10 \%$. Domestic production costs are likely to increase at Yasailand's annual inflation rate.

In addition to the above, components will be imported from the UK (currency £), at the following current cost:

| Year | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Component costs (£ OOOs) | 1,200 | 1,800 | 3,700 | 1,400 |

The costs of components from the UK are fixed and not subject to inflation.
The funds of $\mathrm{Y} \$ 50,000,000$ for Project Alpha will be used to purchase plant and equipment needed for manufacturing purposes. Tax allowable depreciation is available on the value of the plant and equipment at $25 \%$ per year on a reducing balance basis, with a balancing allowance or charge applicable at the end of the project. The plant and equipment is expected to be sold for $\mathrm{Y} \$ 10,000,000$ (post-inflation) at the end of the project.

At the start of every year, Project Alpha will require working capital. In the first year this will be $10 \%$ of the estimated year 1 sales revenue. In subsequent years, the project will require an increase or a reduction in working capital of 15\% for every $\$ 1$ increase or decrease in sales revenue respectively. The working capital is expected to be fully released when Project Alpha ceases.

The expected spot exchange rate between the $Y \$$ and the $£$, in six months' time, is expected to be $Y \$ 3.03$ per $£ 1$. The annual inflation rates are currently $2 \%$ in the UK and $4 \%$ in Yasailand. It can be assumed that these inflation rates will not change for the foreseeable future.

The cost of capital for appraising the base case net present value of Project Alpha is $10 \%$. Okan Co pays tax at an annual rate of $20 \%$. Tax is payable in the same year as the profits it is based on. Okan Co makes sufficient profits from its other activities to take advantage of any tax loss relief.

## Project Beta details

Given below are Project Beta's base case present values, based on the project start date in six months' time, discounted at the project's relevant risk-adjusted all-equity financed discount rate:

| Year | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Present values $(\mathrm{Y} \$ 000 \mathrm{~s})$ | 8,450 | 19,360 | 22,340 | 4,950 |

It can be assumed that any working capital requirements for Project Beta are included in the annual cash flows.
Project Beta's duration has been calculated as 2.43 years, based on its base case present values.
Economic risk and risk categories
One of Okan Co's subsidiary companies in Yasailand, which produces and sells all its products domestically, has still found that it is exposed to economic risk (economic exposure). The directors of the subsidiary believe that this is because Yasailand's government has maintained comparatively higher interest rates, even though the inflation in Yasailand is now under control.

Okan Co categorises the risks inherent in its projects according to the severity of their impact and the frequency of their occurrence, as follows: (i) severe and frequent, (ii) not severe but frequent, (iii) severe but not frequent, and (iv) neither severe nor frequent.

## Required:

(a) Discuss why a company may prefer to use the adjusted present value (APV) method, rather than the net present value (NPV) method.
(b) Prepare a report for the board of directors (BoD) of Okan Co which:
(i) Estimates the minimum amount of debt borrowing Okan Co would require;
(4 marks)
(ii) Estimates

- Project Alpha's and Project Beta's base case NPV, in six months' time, before considering the financing side effects,
(12 marks)
- Project Alpha's and Project Beta's APV, in six months' time, and (6 marks)
- Project Alpha's duration based on its base case present values of cash flows; (2 marks)
(iii) Evaluates and justifies which project Okan Co should choose, basing the decision on the factors Okan Co considers to be important. The evaluation should include a discussion of the assumptions made.
(8 marks)
Professional marks will be awarded in part (b) for the format, structure and presentation of the report.
(4 marks)
(c) Discuss why Okan Co's subsidiary company may be exposed to economic risk (economic exposure) and how it may be managed.
(4 marks)
(d) Discuss how each category of risk, in terms of severity and frequency, may be managed.
(6 marks)


## Section B - BOTH questions are compulsory and MUST be attempted

2 Cadnam Co is a large company in the support services sector.
Cadnam Co's most recent annual report, for the year ended 31 December 20x5, acknowledged challenges for the company, including financing the major investment programme required to meet its clients' increasing expectations. Cadnam Co also faced upward pressure on employment costs, fuelled by a 'fair wage' campaign which adversely compared wage rises in the support services sector with increases in dividends and directors' remuneration, and a consequent government enquiry into low pay in the sector.

Cadnam Co's board, however, was confident that the company would be able to renew a number of large contracts which were coming up for review. The report stressed the strength of Cadnam Co's senior management team as a vital success factor. Directors' remuneration packages thus reflected the need to retain its directors in a competitive labour market at senior level.

In the stakeholder engagement section of its annual report, Cadnam Co highlighted that it had fulfilled its aim of guaranteeing investors a consistent rise in dividends and its board was confident that Cadnam Co would be able to maintain the recent rate of dividend increase. The report also stated that Cadnam Co was looking to publish a full integrated report over the next couple of years.

## Dividend policy

At Cadnam Co's last annual general meeting, there were no questions about the level of profits, dividends or directors' remuneration. However, a recent investment analysts' report on the support services sector highlighted Cadnam Co as a company which might have problems in the next few years. The report suggested that Cadnam Co's investment and dividend policies could not both be maintained. It highlighted one of Cadnam Co's principal competitors, Holmsley Co, as a company whose policies it believed would sustain long-term growth. It highlighted directors' remuneration as an area where Holmsley Co's policies were more likely to encourage long-term value creation and share price increases than Cadnam Co's policies.
Cadnam Co's board is currently considering the comments made by the investment analysts, and also assessing what the dividend for 20X6 should be.

Cadnam Co

|  | $20 \times 2$ | $20 \times 3$ | $20 \times 4$ | $20 \times 5$ |
| :--- | :---: | :---: | :---: | :---: |
|  | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ |
|  | 1,380 | 1,490 | 1,550 | 1,580 |
| Profit after tax | 765 | 840 | 925 | 1,020 |
| Dividends | 282 | 312 | 584 | 864 |
| Investment in additional assets | $\$ 4 \cdot 88$ | $\$ 5 \cdot 35$ | $\$ 5 \cdot 61$ | $\$ 5 \cdot 75$ |
| Share price (\$) |  |  |  |  |
| Gearing (debt/(debt + equity)) <br> (market value) $\times 100 \%$ | $33 \cdot 0 \%$ | $33 \cdot 2 \%$ | $35 \cdot 0 \%$ | $38 \cdot 8 \%$ |
| Holmsley Co |  |  |  |  |
|  | $20 \times 2$ | $20 \times 3$ | $20 \times 4$ | $20 \times 5$ |
|  | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ |
|  | 1,485 | 1,590 | 1,700 | 1,830 |
| Profit after tax | 560 | 590 | 621 | 654 |
| Dividends | 595 | 625 | 660 | 690 |
| Investment in additional assets | $\$ 5 \cdot 04$ | $\$ 5 \cdot 23$ | $\$ 5 \cdot 55$ | $\$ 5 \cdot 93$ |
| Share price |  |  |  |  |
| Gearing (debt/(debt + equity)) | $35 \cdot 1 \%$ | $35 \cdot 2 \%$ | $34 \cdot 9 \%$ | $34 \cdot 7 \%$ |
| (market value) $\times 100 \%$ |  |  |  |  |

Average gearing in the support services sector since 20X1 has been stable at around $34 \%$. There have been no changes in the issued share capital of Cadnam Co and Holmsley Co since 20X1.

Directors' remuneration

Cadnam Co
Average salary executive director
Performance bonus
Loyalty bonus
Share options
\$550,000
Maximum 25\% of salary
Maximum 10\% of salary
None

Holmsley Co
\$550,000
Maximum 30\% of salary
None
Options to be exercised on 31 December 20X8 at an exercise price of $\$ 7 \cdot 00$

## Cadnam Co 20X6 forecast

Forecasts prepared by Cadnam Co's finance director for $20 \times 6$ predict that:

- Cadnam Co's pre-tax operating profit for 20X6 will be $\$ 2,678 \mathrm{~m}$, an increase of $3 \%$ compared with $20 \times 5$. The operating profit margin will be $2 \%$, the same as for 20X5.
- The tax rate will be 30\%.
- Average debt in $20 \times 6$ will be $\$ 10,250 \mathrm{~m}$ and predicted year-end gearing will be $41 \cdot 3 \%$. The average pre-tax interest rate on the debt will be $8 \%$.
- The investment required to keep the non-current asset base at its present productive capacity in $20 \times 6$ will be $\$ 2,430 \mathrm{~m}$, which has been included in the calculation of operating profit as depreciation.
- Investment required in additional assets in 20X6 will be $\$ 0.25$ for every $\$ 1$ increase in revenue.


## Required:

(a) Calculate the forecast dividend capacity of Cadnam Co for 20X6.
(b) Discuss the viability and financial impacts of Cadnam Co seeking to maintain its current dividend policy, supporting your answers with relevant calculations.

Note: 6 marks are available for calculations in part (b).
(c) Discuss the governance and ethical issues associated with Cadnam Co's dividend and directors' remuneration policies.
(8 marks)
(25 marks)

3 A new client has approached you for advice on a potential acquisition. Kerrin Co is a consumer electronics manufacturer and retailer. The company obtained a listing eight years ago with the founders retaining a $20 \%$ stake in the business. Whilst Kerrin Co had previously experienced rapid growth in earnings before tax, problems arose soon after the listing as competition intensified. Although the company remains profitable, annual growth has declined significantly and is currently $3 \%$.

The board is concerned by the lack of future growth opportunities. The current share price reflects these concerns, trading well below the offer price of eight years ago. In response, the directors have decided to invest in a market development strategy for future growth, utilising significant cash reserves to acquire companies in other areas of the country where competition is less intense. The board has identified a potential target, Danton Co.

## Danton Co

Danton Co is a privately owned consumer electronics company, established ten years ago. Significant unrelieved losses were incurred in the early years of development although the company is now profitable and achieving growth in earnings before tax of $6 \%$ per year. However, cash reserves are low. Access to capital has acted as a severe constraint on Danton Co's reinvestment potential throughout this period. The founders and their families own $60 \%$ of the shares with the balance held by a venture capitalist organisation, which acquired its equity stake around six years ago.

## Acquisition information

Kerrin Co's board is keen to ensure that Danton Co's founders remain as directors after the acquisition and the company has sufficient cash reserves to purchase Danton Co outright.

Early discussions between the directors of both companies suggest Danton Co's shareholders would approve a cash offer of $\$ 13 \cdot 10$ per share. As an alternative, the board is considering a share-for-share exchange to fund the acquisition in order to preserve cash for future acquisitions and dividend payments. Recent mergers have attracted an acquisition premium of around $25 \%-30 \%$ and Danton Co's directors indicated their shareholders would be expecting a premium towards the higher end of this scale for a share-for-share offer. Kerrin Co has therefore asked you to design a share-for-share offer scheme which will allow for a $30 \%$ acquisition premium. You have been provided with extracts from the latest financial statements for both companies.

Extracts from the most recent financial statements

|  | Kerrin Co | Danton Co |
| :--- | :---: | :---: |
|  | $\$ \mathrm{~m}$ | $\$ \mathrm{~m}$ |
| Operating profit | 448.6 | $201 \cdot 8$ |
| Earnings before tax | 381.9 | 116.3 |

## Additional financial information

The book value of Kerrin Co's $\$ 0.50$ ordinary shares is $\$ 375 \mathrm{~m}$. These shares are currently trading at $\$ 5.28$ and the finance director expects the price earnings (PE) ratio to increase by $10 \%$ if the acquisition proceeds.

Danton Co upgraded its main manufacturing facility during the previous year and expects to make annual pre-tax cost savings of $\$ 2.5 \mathrm{~m}$ from the start of the current financial year. The book value of Danton Co's $\$ 0.25$ ordinary shares is $\$ 35 \mathrm{~m}$. Based on an analysis of companies of a comparable size and cost structure, it is estimated that Danton Co's PE ratio is $20 \%$ higher than Kerrin Co's current PE ratio.

Kerrin Co's chief executive officer estimates annual pre-tax revenue and cost synergies of $\$ 15 \cdot 2 \mathrm{~m}$ to arise as a result of the acquisition. In addition, the finance director anticipates annual pre-tax financial synergies of $\$ 5.3 \mathrm{~m}$ although she insists this is a cautious estimate after reading an article on recent merger and acquisition activity where post-acquisition synergies have either been overestimated or failed to materialise.

The rate of corporation tax relevant to both companies is $20 \%$.

## Required:

(a) Discuss possible sources of financial synergy arising from Kerrin Co's acquisition of Danton Co and comment on the finance director's concern that synergy is often overestimated, including any steps which could be taken by Kerrin Co's board to address this problem.
(b) Advise the directors on a suitable share-for-share exchange offer which meets the criteria specified by Danton Co's shareholders and calculate the effect of the cash and share-for-share offers on the post-acquisition wealth of both Kerrin Co's and Danton Co's shareholders.
(c) Discuss the likely reaction of Kerrin Co's and Danton Co's shareholders to the cash and share-for-share offers.

## Formulae

Modigliani and Miller Proposition 2 (with tax)

$$
k_{e}=k_{e}^{i}+(1-T)\left(k_{e}^{i}-k_{d}\right) \frac{V_{d}}{V_{e}}
$$

## The Capital Asset Pricing Model

$$
\mathrm{E}\left(\mathrm{r}_{\mathrm{i}}\right)=\mathrm{R}_{\mathrm{f}}+\beta_{\mathrm{i}}\left(\mathrm{E}\left(\mathrm{r}_{\mathrm{m}}\right)-\mathrm{R}_{\mathrm{f}}\right)
$$

The asset beta formula

$$
\beta_{\mathrm{a}}=\left[\frac{\mathrm{V}_{\mathrm{e}}}{\left(\mathrm{~V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{e}}\right]+\left[\frac{\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})}{\left(\mathrm{V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{d}}\right]
$$

The Growth Model

$$
P_{o}=\frac{D_{0}(1+g)}{\left(r_{e}-g\right)}
$$

## Gordon's growth approximation

$$
\mathrm{g}=\mathrm{br} \mathrm{r}_{\mathrm{e}}
$$

The weighted average cost of capital

$$
\text { WACC }=\left[\frac{V_{e}}{V_{e}+V_{d}}\right] k_{e}+\left[\frac{V_{d}}{V_{e}+V_{d}}\right] k_{d}(1-T)
$$

## The Fisher formula

$$
(1+i)=(1+r)(1+h)
$$

Purchasing power parity and interest rate parity

$$
S_{1}=S_{0} \times \frac{\left(1+h_{c}\right)}{\left(1+h_{b}\right)} \quad F_{0}=S_{0} \times \frac{\left(1+i_{c}\right)}{\left(1+i_{b}\right)}
$$

Modified Internal Rate of Return

$$
M I R R=\left[\frac{P V_{R}}{P V_{I}}\right]^{\frac{1}{n}}\left(1+r_{e}\right)-1
$$

The Black-Scholes option pricing model

$$
c=P_{a} N\left(d_{1}\right)-P_{e} N\left(d_{2}\right) e^{-r t}
$$

Where:

$$
\begin{aligned}
& d_{1}=\frac{\ln \left(P_{a} / P_{e}\right)+\left(r+0.5 s^{2}\right) t}{s \sqrt{t}} \\
& d_{2}=d_{1}-s \sqrt{t}
\end{aligned}
$$

The Put Call Parity relationship

$$
p=c-P_{a}+P_{e} e^{-r t}
$$

## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
Where $r=$ discount rate
$\mathrm{n}=$ number of periods until payment
Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

| Where | $r=$ discount rate |
| :--- | :--- |
|  | $n=$ number of periods |

Discount rate (r)
Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | $2 \cdot 941$ | $2 \cdot 884$ | $2 \cdot 829$ | $2 \cdot 775$ | $2 \cdot 723$ | 2.673 | $2 \cdot 624$ | $2 \cdot 577$ | 2.531 | $2 \cdot 487$ | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | $3 \cdot 387$ | $3 \cdot 312$ | 3.240 | $3 \cdot 170$ | 4 |
| 5 | 4.853 | $4 \cdot 713$ | 4.580 | 4.452 | $4 \cdot 329$ | $4 \cdot 212$ | $4 \cdot 100$ | 3.993 | 3.890 | $3 \cdot 791$ | 5 |
| 6 | $5 \cdot 795$ | $5 \cdot 601$ | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | 6.728 | 6.472 | 6.230 | 6.002 | 5.786 | 5.582 | $5 \cdot 389$ | $5 \cdot 206$ | 5.033 | $4 \cdot 868$ | 7 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | 6.210 | 5.971 | $5 \cdot 747$ | 5.535 | $5 \cdot 335$ | 8 |
| 9 | 8.566 | $8 \cdot 162$ | 7.786 | 7.435 | 7.108 | 6.802 | $6 \cdot 515$ | 6.247 | 5.995 | $5 \cdot 759$ | 9 |
| 10 | $9 \cdot 471$ | 8.983 | 8.530 | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | $6 \cdot 418$ | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 368$ | 9.787 | $9 \cdot 253$ | 8.760 | $8 \cdot 306$ | 7.887 | $7 \cdot 499$ | $7 \cdot 139$ | 6.805 | 6.495 | 11 |
| 12 | $11 \cdot 255$ | $10 \cdot 575$ | 9.954 | $9 \cdot 385$ | $8 \cdot 863$ | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 134$ | $11 \cdot 348$ | $10 \cdot 635$ | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | $7 \cdot 487$ | $7 \cdot 103$ | 13 |
| 14 | 13.004 | $12 \cdot 106$ | 11.296 | $10 \cdot 563$ | $9 \cdot 899$ | 9.295 | $8 \cdot 745$ | 8.244 | 7.786 | $7 \cdot 367$ | 14 |
| 15 | $13 \cdot 865$ | $12 \cdot 849$ | 11.938 | $11 \cdot 118$ | $10 \cdot 380$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | $0 \cdot 862$ | $0 \cdot 855$ | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | $2 \cdot 402$ | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | 2.974 | 2.914 | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | 2.639 | 2.589 | 4 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | 4.231 | 4.111 | 3.998 | 3.889 | $3 \cdot 784$ | 3.685 | 3.589 | 3.498 | 3.410 | $3 \cdot 326$ | 6 |
| 7 | $4 \cdot 712$ | 4.564 | 4.423 | $4 \cdot 288$ | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 | 7 |
| 8 | $5 \cdot 146$ | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | $4 \cdot 207$ | 4.078 | 3.954 | 3.837 | 8 |
| 9 | 5.537 | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | 4.772 | $4 \cdot 607$ | $4 \cdot 451$ | 4.303 | $4 \cdot 163$ | 4.031 | 9 |
| 10 | 5.889 | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | 4.833 | $4 \cdot 659$ | 4.494 | $4 \cdot 339$ | $4 \cdot 192$ | 10 |
| 11 | $6 \cdot 207$ | 5.938 | $5 \cdot 687$ | $5 \cdot 453$ | 5.234 | 5.029 | $4 \cdot 836$ | $4 \cdot 656$ | $4 \cdot 486$ | 4.327 | 11 |
| 12 | 6.492 | $6 \cdot 194$ | 5.918 | $5 \cdot 660$ | $5 \cdot 421$ | $5 \cdot 197$ | $4 \cdot 988$ | 4.793 | $4 \cdot 611$ | 4.439 | 12 |
| 13 | 6.750 | $6 \cdot 424$ | 6.122 | $5 \cdot 842$ | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | 6.628 | $6 \cdot 302$ | 6.002 | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | 4.611 | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | 5.847 | 5.575 | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | 4.675 | 15 |

Standard normal distribution table

|  | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | $0 \cdot 09$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| $0 \cdot 1$ | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| $0 \cdot 2$ | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | $0 \cdot 1026$ | $0 \cdot 1064$ | $0 \cdot 1103$ | $0 \cdot 1141$ |
| $0 \cdot 3$ | $0 \cdot 1179$ | $0 \cdot 1217$ | $0 \cdot 1255$ | $0 \cdot 1293$ | $0 \cdot 1331$ | $0 \cdot 1368$ | $0 \cdot 1406$ | 0.1443 | 0.1480 | $0 \cdot 1517$ |
| 0.4 | $0 \cdot 1554$ | $0 \cdot 1591$ | $0 \cdot 1628$ | $0 \cdot 1664$ | $0 \cdot 1700$ | $0 \cdot 1736$ | $0 \cdot 1772$ | $0 \cdot 1808$ | $0 \cdot 1844$ | $0 \cdot 1879$ |
| 0.5 | $0 \cdot 1915$ | 0.1950 | $0 \cdot 1985$ | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | 0.3023 | $0 \cdot 3051$ | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | $0 \cdot 3159$ | 0.3186 | $0 \cdot 3212$ | $0 \cdot 3238$ | $0 \cdot 3264$ | $0 \cdot 3289$ | 0.3315 | 0.3340 | $0 \cdot 3365$ | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | $0 \cdot 3508$ | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| $1 \cdot 1$ | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| $1 \cdot 2$ | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | $0 \cdot 3997$ | 0.4015 |
| $1 \cdot 3$ | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | $0 \cdot 4222$ | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| $2 \cdot 1$ | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| $2 \cdot 2$ | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| $2 \cdot 3$ | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| $2 \cdot 5$ | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| $2 \cdot 6$ | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| $2 \cdot 7$ | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| $2 \cdot 9$ | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

This table can be used to calculate $N(d)$, the cumulative normal distribution functions needed for the Black-Scholes model of option pricing. If $d_{i}>0$, add 0.5 to the relevant number above. If $d_{i}<0$, subtract the relevant number above from 0.5 .

## End of Question Paper

